Amendments to the Specification

Beginning on page 6, line 11 to page 8, line 5, please replace the equations with the following more legible equations:

Equations:

$$\frac{\partial}{\partial t} \left(rw \sqrt{1 + \left(\frac{\partial r}{\partial z}\right)^2} \right) + \frac{\partial}{\partial z} (rwv) = 0, \tag{1}$$

Where,

$$t = \frac{\overline{t}\overline{v_0}}{\overline{r_0}}, \quad z = \frac{\overline{z}}{\overline{r_0}}, \quad r = \frac{\overline{r}}{\overline{r_0}}, \quad v = \frac{\overline{v}}{\overline{v_0}}, \quad w = \frac{\overline{w}}{\overline{w_0}}$$

Axial direction:

$$\begin{split} \frac{2rw[(\tau_{11}-\tau_{22})]+2r\sigma_{\mathit{surf}}}{\sqrt{1+(\partial r/\partial z)^2}}+B(r_F^2-r^2) - \\ 2C_{\mathit{gr}}\int_0^{2_L}\!\!rw\sqrt{1+(\partial r/\partial z)^2}\,dz - 2\int_0^{2_L}\!\!r\,T_{\mathit{drag}}d_z = T_z \end{split} \tag{2}$$

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Where,

$$T_z = rac{\overline{T}_z}{2\pi\eta_0\overline{w}_0\overline{v}_0}, \quad B = rac{\overline{r}_0^2 \Delta P}{2\eta_0\overline{w}_0\overline{v}_0},$$

$$\Delta P = rac{A}{\int_0^{z_L} \pi \overline{r}^2 d\overline{z}} - P_a, \quad \tau_{ij} = rac{\overline{\tau}_{ij}\overline{r}_0}{2\eta_0\overline{v}_0}.$$

$$C_{\mathit{gr}} = \frac{\rho g \overline{r_0^2}}{2 \eta_0 \overline{v_0}}, T_{\mathit{drag}} = \frac{\overline{T_{\mathit{drag}}} \overline{r_0^2}}{2 \eta_0 \overline{v_0} \overline{w_0}}, \sigma_{\mathit{surf}} = \frac{\overline{\sigma_{\mathit{surf}} r_0}}{2 \eta_0 \overline{v_0} \overline{w_0}}$$

Circumferential direction:

$$B = (\frac{[-w(\tau_{11} - \tau_{22}) + 2\sigma_{\mathit{surf}}](\partial^2 r / \partial z^2)}{[1 + (\partial r / \partial z)^2]^{3/2}} + \frac{w(\tau_{33} - \tau_{22}) + 2\sigma_{\mathit{surf}}}{\tau \sqrt{1 + (\partial r / \partial z)^2}} - C_{\mathit{gr}} \frac{\partial r / \partial z}{\sqrt{1 + (\partial r / \partial z)^2}})$$

(3)

Constitutive Equation:

$$K\tau + De\left(\frac{\partial \tau}{\partial t} + \mathbf{v} \cdot \nabla \tau - L \cdot \tau - \tau \cdot L^{\mathrm{T}}\right) = 2\frac{De}{De_0}D,$$
(4)

where
$$K = \exp[\varepsilon De \operatorname{tr} \tau]$$
, $L = \nabla v - \xi D$, $2D = (\nabla v + \nabla v T)$, $De_0 = \frac{\lambda v_0}{r_0}$, $De = De_0 \exp\left[k\left(\frac{1}{\theta} - 1\right)\right]$.

Energy Equation:

$$\frac{\partial \theta}{\partial t} + \frac{v}{\sqrt{1 + (\partial r/\partial z)^2}} \frac{\partial \theta}{\partial z} + \frac{U}{w} (\theta - \theta_c) + \frac{E}{w} (\theta^4 - \theta_\infty^4) = 0,$$
(5)

Where,

$$\begin{split} \theta &= \frac{\overline{\theta}}{\theta_0}, \quad \theta_{\rm c} = \frac{\overline{\theta}_{\rm c}}{\theta_0}, \quad \theta_{\infty} = \frac{\overline{\theta}_{\infty}}{\theta_0}, \quad U = \frac{\overline{U}\overline{r}_0}{\rho C_P \overline{w}_0 \overline{v}_0}, \\ E &= \frac{\varepsilon_{\rm m} \sigma_{\rm SB} \overline{\theta}_0^4 \overline{r}_0}{\rho C_P \overline{w}_0 \overline{v}_0 \theta_0} \end{split}$$

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Boundary conditions:

$$v = w = r = \theta = 1, \tau = \tau_0 \text{at } z = z_0, (6a)$$

$$\frac{\partial r}{\partial t} + \frac{\partial r}{\partial z} \frac{v}{\sqrt{1 + (\partial r/\partial z)^2}} = 0, \frac{v}{\sqrt{1 + (\partial r/\partial z)^2}} = D_R,$$

$$\theta = \theta_F \text{at } z = z_F. (6b)$$

Beginning on page 12, line 13 to page 14, line 6, please replace the equations with the following more legible equations:

Equations:

$$\frac{\partial}{\partial t} \left(rw \sqrt{1 + \left(\frac{\partial r}{\partial z}\right)^2} \right) + \frac{\partial}{\partial z} (rwv) = 0, \tag{1}$$

Where,

$$t = \frac{\overline{t}\overline{v_0}}{\overline{r_0}}, \quad z = \frac{\overline{z}}{\overline{r_0}}, \quad r = \frac{\overline{r}}{\overline{r_0}}, \quad v = \frac{\overline{v}}{\overline{v_0}}, \quad w = \frac{\overline{w}}{\overline{w_0}}$$

Axial direction:

$$\begin{split} \frac{2rw[(\tau_{11}-\tau_{22})]+2r\sigma_{surf}}{\sqrt{1+(\partial r/\partial z)^2}}+B(r_F^2-r^2)-\\ 2C_{gr}\int_0^{2_L} rw\sqrt{1+(\partial r/\partial z)^2}\,dz-2\int_0^{2_L} r\,T_{drag}d_z=T_z \end{split} \tag{2}$$

Where,

$$\begin{split} T_z &= \frac{\overline{T}_z}{2\pi\eta_0\overline{w}_0\overline{v}_0}, \quad B = \frac{\overline{r}_0^2\,\Delta P}{2\eta_0\overline{w}_0\overline{v}_0}, \\ \Delta P &= \frac{A}{\int_0^{z_{\rm L}}\pi\overline{r}^2\,\mathrm{d}\overline{z}} - P_{\rm a}, \quad \tau_{ij} = \frac{\overline{\tau}_{ij}\overline{r}_0}{2\eta_0\overline{v}_0} \end{split}$$

$$C_{gr} = \frac{\rho g \overline{r_0^2}}{2\eta_0 \overline{v_0}}, T_{drag} = \frac{\overline{T_{drag}} \overline{r_0^2}}{2\eta_0 \overline{v_0} \overline{w_0}}, \sigma_{surf} = \frac{\overline{\sigma_{surf}} \overline{r_0}}{2\eta_0 \overline{v_0} \overline{w_0}}$$

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Circumferential direction:

$$B = \left(\frac{\left[-w(\tau_{11} - \tau_{22}) + 2\sigma_{surf}\right](\partial^{2}r/\partial z^{2})}{\left[1 + (\partial r/\partial z)^{2}\right]^{3/2}} + \frac{w(\tau_{33} - \tau_{22}) + 2\sigma_{surf}}{\tau\sqrt{1 + (\partial r/\partial z)^{2}}} - C_{gr}\frac{\partial r/\partial z}{\sqrt{1 + (\partial r/\partial z)^{2}}}\right)$$

Constitutive Equation:

$$K\tau + De\left(\frac{\partial \tau}{\partial t} + \boldsymbol{v} \cdot \nabla \tau - \boldsymbol{L} \cdot \boldsymbol{\tau} - \boldsymbol{\tau} \cdot \boldsymbol{L}^{\mathrm{T}}\right) = 2\frac{De}{De_0}\boldsymbol{D},\tag{4}$$

where
$$K = \exp[\varepsilon De \operatorname{tr} \tau]$$
, $L = \nabla v - \xi D$, $2D = (\nabla v + \nabla v T)$, $De_0 = \frac{\lambda v_0}{r_0}$, $De = De_0 \exp\left[k\left(\frac{1}{\theta} - 1\right)\right]$.

Energy Equation:

$$\frac{\partial \theta}{\partial t} + \frac{v}{\sqrt{1 + (\partial r/\partial z)^2}} \frac{\partial \theta}{\partial z} + \frac{U}{w} (\theta - \theta_c) + \frac{E}{w} (\theta^4 - \theta_\infty^4) = 0,$$
(5)

Where.

$$\begin{split} \theta &= \frac{\overline{\theta}}{\theta_0}, \quad \theta_{\rm c} = \frac{\overline{\theta}_{\rm c}}{\theta_0}, \quad \theta_{\infty} = \frac{\overline{\theta}_{\infty}}{\theta_0}, \quad U = \frac{\overline{U}\overline{r}_0}{\rho C_P \overline{w}_0 \overline{v}_0}, \\ E &= \frac{\varepsilon_{\rm m} \sigma_{\rm SB} \overline{\theta}_0^4 \overline{r}_0}{\rho C_P \overline{w}_0 \overline{v}_0 \theta_0} \end{split}$$

Boundary conditions:

$$v = w = r = \theta = 1, \tau = \tau_0 \text{at } z = z_0, (6a)$$

$$\frac{\partial r}{\partial t} + \frac{\partial r}{\partial z} \frac{v}{\sqrt{1 + (\partial r/\partial z)^2}} = 0, \frac{v}{\sqrt{1 + (\partial r/\partial z)^2}} = D_R,$$

$$\theta = \theta_F \text{at } z = z_F. (6b)$$